

Diffusion Maps

Generated by Doxygen 1.8.17

1 Namespace Index	1
1.1 Namespace List	1
2 Class Index	3
2.1 Class List	3
3 File Index	5
3.1 File List	5
4 Namespace Documentation	7
4.1 diffusion_maps Namespace Reference	7
4.1.1 Detailed Description	8
4.1.2 Function Documentation	8
4.1.2.1 diffusion_maps()	8
4.2 diffusion_maps::kernel Namespace Reference	9
4.2.1 Detailed Description	9
5 Class Documentation	11
5.1 diffusion_maps::kernel::Gaussian Class Reference	11
5.1.1 Detailed Description	11
5.1.2 Constructor & Destructor Documentation	11
5.1.2.1 Gaussian()	11
5.1.3 Member Function Documentation	12
5.1.3.1 with_gamma()	12
5.1.3.2 with_sigma()	12
5.2 diffusion_maps::Matrix Class Reference	12
5.2.1 Detailed Description	13
5.2.2 Constructor & Destructor Documentation	13
5.2.2.1 Matrix() [1/2]	13
5.2.2.2 Matrix() [2/2]	14
5.2.3 Member Function Documentation	14
5.2.3.1 operator() [1/2]	14
5.2.3.2 operator() [2/2]	15
5.2.3.3 row()	15
5.3 diffusion_maps::SparseMatrix Class Reference	15
5.3.1 Detailed Description	16
5.3.2 Constructor & Destructor Documentation	17
5.3.2.1 SparseMatrix() [1/3]	17
5.3.2.2 SparseMatrix() [2/3]	17
5.3.2.3 SparseMatrix() [3/3]	17
5.3.3 Member Function Documentation	18
5.3.3.1 operator*()	18
5.3.3.2 operator=() [1/2]	18
5.3.3.3 operator=() [2/2]	18

5.4	diffusion_maps::SparseMatrix::Triplet Class Reference	19
5.4.1	Detailed Description	19
5.4.2	Member Function Documentation	19
5.4.2.1	operator<()	19
5.5	diffusion_maps::Vector Class Reference	20
5.5.1	Detailed Description	21
5.5.2	Constructor & Destructor Documentation	21
5.5.2.1	Vector() [1/5]	21
5.5.2.2	Vector() [2/5]	22
5.5.2.3	Vector() [3/5]	22
5.5.2.4	Vector() [4/5]	22
5.5.2.5	Vector() [5/5]	23
5.5.3	Member Function Documentation	23
5.5.3.1	dot()	23
5.5.3.2	inv_sqrt()	23
5.5.3.3	operator!=()	24
5.5.3.4	operator*()	24
5.5.3.5	operator*=(())	24
5.5.3.6	operator+()	25
5.5.3.7	operator+=(())	25
5.5.3.8	operator-() [1/2]	25
5.5.3.9	operator-() [2/2]	26
5.5.3.10	operator-=()	26
5.5.3.11	operator/()	27
5.5.3.12	operator/=()	27
5.5.3.13	operator=() [1/2]	27
5.5.3.14	operator=() [2/2]	28
5.5.3.15	operator==(())	28
5.5.3.16	operator[]() [1/2]	28
5.5.3.17	operator[]() [2/2]	29
6	File Documentation	31
6.1	include/diffusion_maps/diffusion_maps.hpp File Reference	31
6.1.1	Detailed Description	32
6.2	include/diffusion_maps/kernel.hpp File Reference	32
6.2.1	Detailed Description	32
6.3	include/diffusion_maps/matrix.hpp File Reference	32
6.3.1	Detailed Description	33
6.4	include/diffusion_maps/sparse_matrix.hpp File Reference	33
6.4.1	Detailed Description	33
6.5	include/diffusion_maps/vector.hpp File Reference	33
6.5.1	Detailed Description	34

Chapter 1

Namespace Index

1.1 Namespace List

Here is a list of all documented namespaces with brief descriptions:

diffusion_maps		
	Namespace for everything related to diffusion maps	7
diffusion_maps::kernel		
	Diffusion kernels	9

Chapter 2

Class Index

2.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

diffusion_maps::kernel::Gaussian	
Gaussian kernel	11
diffusion_maps::Matrix	
Matrix of doubles that may or may not own its data	12
diffusion_maps::SparseMatrix	
Sparse matrix in the CSR format	15
diffusion_maps::SparseMatrix::Triplet	
A non-zero element of a sparse matrix as a (i, j, value) triplet	19
diffusion_maps::Vector	
Vector	20

Chapter 3

File Index

3.1 File List

Here is a list of all documented files with brief descriptions:

include/diffusion_maps/ diffusion_maps.hpp	
Diffusion maps algorithm	31
include/diffusion_maps/ kernel.hpp	
Diffusion kernels	32
include/diffusion_maps/ matrix.hpp	
Matrix	32
include/diffusion_maps/ sparse_matrix.hpp	
Sparse matrix	33
include/diffusion_maps/ vector.hpp	
Vector	33

Chapter 4

Namespace Documentation

4.1 diffusion_maps Namespace Reference

Namespace for everything related to diffusion maps.

Namespaces

- [kernel](#)
Diffusion kernels.

Classes

- class [Matrix](#)
Matrix of doubles that may or may not own its data.
- class [SparseMatrix](#)
Sparse matrix in the CSR format.
- class [Vector](#)
Vector.

Functions

- `template<typename R >`
`Matrix diffusion_maps (const Matrix &data, std::size_t n_components, const std::function< double(const Vector &, const Vector &)> &kernel, double diffusion_time, R &rng, double kernel_epsilon=DEFAULT_KERNEL_EPSILON, double eig_solver_tol=DEFAULT_EIG_SOLVER_TOL, unsigned eig_solver_max_iter=DEFAULT_EIG_SOLVER_MAX_ITER)`
Diffusion maps.

Variables

- `constexpr double DEFAULT_KERNEL_EPSILON = 1e-6`
Default kernel epsilon for the `diffusion_maps()` function.
- `constexpr double DEFAULT_EIG_SOLVER_TOL = 1e-6`
Default tolerance of the eigendecomposition solver for the `diffusion_maps()` function.
- `constexpr unsigned DEFAULT_EIG_SOLVER_MAX_ITER = 100000`
Default maximum number of iterations of the eigendecomposition solver for the `diffusion_maps()` function.

4.1.1 Detailed Description

Namespace for everything related to diffusion maps.

4.1.2 Function Documentation

4.1.2.1 diffusion_maps()

```
template<typename R >
Matrix diffusion_maps::diffusion_maps (
    const Matrix & data,
    std::size_t n_components,
    const std::function< double(const Vector &, const Vector &)> & kernel,
    double diffusion_time,
    R & rng,
    double kernel_epsilon = DEFAULT_KERNEL_EPSILON,
    double eig_solver_tol = DEFAULT_EIG_SOLVER_TOL,
    unsigned eig_solver_max_iter = DEFAULT_EIG_SOLVER_MAX_ITER )
```

Diffusion maps.

Template Parameters

<i>R</i>	The type of the random number generator.
----------	--

Parameters

in	<i>data</i>	The data matrix where each row is a data point.
in	<i>n_components</i>	The dimension of the projected subspace.
in	<i>kernel</i>	The kernel function.
in	<i>diffusion_time</i>	The diffusion time.
in, out	<i>rng</i>	The random number generator.
in	<i>kernel_epsilon</i>	The value below which the output of the kernel would be treated as zero.
in	<i>eig_solver_tol</i>	The tolerance of the eigendecomposition solver.
in	<i>eig_solver_max_iter</i>	The maximum number of iterations of the eigendecomposition solver.

Returns

The lower-dimensional embedding of the data in the diffusion space.

Exceptions

<i>std::invalid_argument</i>	If <i>n_components</i> is greater than the number of data points minus 1.
<i>std::invalid_argument</i>	If <i>diffusion_time</i> is negative.

4.2 diffusion_maps::kernel Namespace Reference

Diffusion kernels.

Classes

- class [Gaussian](#)
Gaussian kernel.

4.2.1 Detailed Description

Diffusion kernels.

Chapter 5

Class Documentation

5.1 diffusion_maps::kernel::Gaussian Class Reference

[Gaussian](#) kernel.

```
#include <diffusion_maps/kernel.hpp>
```

Public Member Functions

- [Gaussian](#) (const double [gamma](#))
Constructs a [Gaussian](#) kernel with the given parameter γ .
- double [operator\(\)](#) (const [Vector](#) &x, const [Vector](#) &y) const
Evaluates the kernel function.

Static Public Member Functions

- static [Gaussian with_gamma](#) (const double [gamma](#))
Constructs a [Gaussian](#) kernel with the given parameter γ .
- static [Gaussian with_sigma](#) (const double sigma)
Constructs a [Gaussian](#) kernel with the given σ .

Public Attributes

- double [gamma](#)
Kernel parameter $\gamma = 1 / 2\sigma^2$.

5.1.1 Detailed Description

[Gaussian](#) kernel.

5.1.2 Constructor & Destructor Documentation

5.1.2.1 [Gaussian\(\)](#)

```
diffusion_maps::kernel::Gaussian::Gaussian (  
    const double gamma ) [inline]
```

Constructs a [Gaussian](#) kernel with the given parameter γ .

Parameters

in	<i>gamma</i>	Kernel parameter $\gamma = 1 / 2\sigma^2$.
----	--------------	---

5.1.3 Member Function Documentation

5.1.3.1 with_gamma()

```
static Gaussian diffusion_maps::kernel::Gaussian::with_gamma (
    const double gamma ) [inline], [static]
```

Constructs a [Gaussian](#) kernel with the given parameter γ .

Parameters

in	<i>gamma</i>	Kernel parameter $\gamma = 1 / 2\sigma^2$.
----	--------------	---

5.1.3.2 with_sigma()

```
static Gaussian diffusion_maps::kernel::Gaussian::with_sigma (
    const double sigma ) [inline], [static]
```

Constructs a [Gaussian](#) kernel with the given σ .

Parameters

in	<i>sigma</i>	Kernel parameter σ .
----	--------------	-----------------------------

The documentation for this class was generated from the following file:

- [include/diffusion_maps/kernel.hpp](#)

5.2 diffusion_maps::Matrix Class Reference

[Matrix](#) of doubles that may or may not own its data.

```
#include <diffusion_maps/matrix.hpp>
```

Public Member Functions

- [Matrix](#) (const std::size_t [n_rows](#), const std::size_t [n_cols](#))
Constructs an owning matrix of the given dimensions with uninitialized elements.
- [Matrix](#) (double *const [data](#), const std::size_t [n_rows](#), const std::size_t [n_cols](#), const std::size_t [row_stride](#), const std::size_t [col_stride](#))
Constructs a non-owning matrix.
- double * [data](#) ()
The data array.
- const double * [data](#) () const
The data array.
- std::size_t [n_rows](#) () const
The number of rows.
- std::size_t [n_cols](#) () const
The number of columns.
- std::size_t [row_stride](#) () const
The stride in the row dimension.
- std::size_t [col_stride](#) () const
The stride in the column dimension.
- double & [operator](#)() (const std::size_t [i](#), const std::size_t [j](#))
Returns the ([i](#) , [j](#))-th element without bounds checking.
- double [operator](#)() (const std::size_t [i](#), const std::size_t [j](#)) const
Returns the ([i](#) , [j](#))-th element without bounds checking.
- [Vector row](#) (const std::size_t [i](#)) const
Returns the [i](#) -th row without bounds checking.

Protected Attributes

- std::variant< std::unique_ptr< double[]>, double * > [_data](#)
The data array.
- std::size_t [_n_rows](#)
The number of rows.
- std::size_t [_n_cols](#)
The number of columns.
- std::size_t [_row_stride](#)
The stride in the row dimension.
- std::size_t [_col_stride](#)
The stride in the column dimension.

5.2.1 Detailed Description

[Matrix](#) of doubles that may or may not own its data.

5.2.2 Constructor & Destructor Documentation

5.2.2.1 Matrix() [1/2]

```
diffusion_maps::Matrix::Matrix (
    const std::size_t n\_rows,
    const std::size_t n\_cols ) [inline]
```

Constructs an owning matrix of the given dimensions with uninitialized elements.

Parameters

in	<i>n_rows</i>	The number of rows.
in	<i>n_cols</i>	The number of columns.

5.2.2.2 Matrix() [2/2]

```
diffusion_maps::Matrix::Matrix (
    double *const data,
    const std::size_t n_rows,
    const std::size_t n_cols,
    const std::size_t row_stride,
    const std::size_t col_stride ) [inline]
```

Constructs a non-owning matrix.

Parameters

in	<i>data</i>	The data array.
in	<i>n_rows</i>	The number of rows.
in	<i>n_cols</i>	The number of columns.
in	<i>row_stride</i>	The stride in the row dimension.
in	<i>col_stride</i>	The stride in the column dimension.

5.2.3 Member Function Documentation**5.2.3.1 operator() [1/2]**

```
double& diffusion_maps::Matrix::operator() (
    const std::size_t i,
    const std::size_t j ) [inline]
```

Returns the (*i* , *j*)-th element without bounds checking.

Parameters

in	<i>i</i>	The row index.
in	<i>j</i>	The column index.

Returns

The (*i* , *j*)-th element.

5.2.3.2 operator() [2/2]

```
double diffusion_maps::Matrix::operator() (
    const std::size_t i,
    const std::size_t j ) const [inline]
```

Returns the (i , j)-th element without bounds checking.

Parameters

in	i	The row index.
in	j	The column index.

Returns

The (i , j)-th element.

5.2.3.3 row()

```
Vector diffusion_maps::Matrix::row (
    const std::size_t i ) const [inline]
```

Returns the i -th row without bounds checking.

Parameters

in	i	The row index.
----	-----	----------------

Returns

The i -th row.

The documentation for this class was generated from the following file:

- [include/diffusion_maps/matrix.hpp](#)

5.3 diffusion_maps::SparseMatrix Class Reference

Sparse matrix in the CSR format.

```
#include <diffusion_maps/sparse_matrix.hpp>
```

Classes

- class [Triplet](#)
A non-zero element of a sparse matrix as a (i , j , value) triplet.

Public Member Functions

- [SparseMatrix](#) ()
Constructs an empty 0×0 matrix.
- [SparseMatrix](#) (const std::size_t n_rows, const std::size_t n_cols, std::vector< [Triplet](#) > &triplets)
Constructs a sparse matrix from a vector of triplets.
- [SparseMatrix](#) (const [SparseMatrix](#) &other)
Copy constructor.
- [SparseMatrix](#) ([SparseMatrix](#) &&other) noexcept
Move constructor. The moved-from matrix is set to an empty 0×0 matrix.
- virtual [~SparseMatrix](#) ()=default
Destructor.
- [SparseMatrix](#) & [operator=](#) (const [SparseMatrix](#) &other)
Copy assignment operator.
- [SparseMatrix](#) & [operator=](#) ([SparseMatrix](#) &&other)
Move assignment operator. The moved-from matrix is set to an empty 0×0 matrix.
- std::size_t [n_rows](#) () const
The number of rows.
- std::size_t [n_cols](#) () const
The number of columns.
- std::size_t [n_nz](#) () const
The number of non-zero elements.
- double * [data](#) ()
The data array.
- const double * [data](#) () const
The data array.
- const std::size_t * [col_ixs](#) () const
The column indices array.
- const std::size_t * [row_ixs](#) () const
The row indices array.
- [Vector operator*](#) (const [Vector](#) &v) const
Matrix-vector multiplication.

Protected Attributes

- std::size_t [_n_rows](#)
The number of rows.
- std::size_t [_n_cols](#)
The number of columns.
- std::unique_ptr< double[] > [_data](#)
The data array of the matrix.
- std::unique_ptr< std::size_t[] > [_col_ixs](#)
The column indices of each non-zero element.
- std::unique_ptr< std::size_t[] > [_row_ixs](#)
The indices of each row.

5.3.1 Detailed Description

Sparse matrix in the CSR format.

5.3.2 Constructor & Destructor Documentation

5.3.2.1 SparseMatrix() [1/3]

```
diffusion_maps::SparseMatrix::SparseMatrix (
    const std::size_t n_rows,
    const std::size_t n_cols,
    std::vector< Triplet > & triplets ) [inline]
```

Constructs a sparse matrix from a vector of triplets.

Parameters

in	<i>n_rows</i>	The number of rows.
in	<i>n_cols</i>	The number of columns.
in, out	<i>triplets</i>	The vector of triplets. Elements are sorted in-place.

5.3.2.2 SparseMatrix() [2/3]

```
diffusion_maps::SparseMatrix::SparseMatrix (
    const SparseMatrix & other ) [inline]
```

Copy constructor.

Parameters

in	<i>other</i>	The sparse matrix to copy.
----	--------------	----------------------------

5.3.2.3 SparseMatrix() [3/3]

```
diffusion_maps::SparseMatrix::SparseMatrix (
    SparseMatrix && other ) [inline], [noexcept]
```

Move constructor. The moved-from matrix is set to an empty 0×0 matrix.

Parameters

in, out	<i>other</i>	The sparse matrix to move.
---------	--------------	----------------------------

5.3.3 Member Function Documentation

5.3.3.1 operator*()

```
Vector diffusion_maps::SparseMatrix::operator* (
    const Vector & v ) const [inline]
```

Matrix-vector multiplication.

Parameters

in	v	The vector to multiply.
----	---	-------------------------

Returns

The result of the multiplication.

Exceptions

<code>std::invalid_argument</code>	If the dimensions are incompatible.
------------------------------------	-------------------------------------

5.3.3.2 operator=() [1/2]

```
SparseMatrix& diffusion_maps::SparseMatrix::operator= (
    const SparseMatrix & other ) [inline]
```

Copy assignment operator.

Parameters

in	<i>other</i>	The sparse matrix to copy.
----	--------------	----------------------------

Returns

A reference to this sparse matrix.

5.3.3.3 operator=() [2/2]

```
SparseMatrix& diffusion_maps::SparseMatrix::operator= (
    SparseMatrix && other ) [inline]
```

Move assignment operator. The moved-from matrix is set to an empty 0×0 matrix.

Parameters

<code>in, out</code>	<i>other</i>	The sparse matrix to move.
----------------------	--------------	----------------------------

Returns

A reference to this sparse matrix.

The documentation for this class was generated from the following file:

- [include/diffusion_maps/sparse_matrix.hpp](#)

5.4 diffusion_maps::SparseMatrix::Triplet Class Reference

A non-zero element of a sparse matrix as a (i, j, value) triplet.

```
#include <diffusion_maps/sparse_matrix.hpp>
```

Public Member Functions

- `bool operator<` (const [Triplet](#) &other) const
Less-than comparison operator. Compares the row and column indices.

Public Attributes

- `std::size_t row`
The row index.
- `std::size_t col`
The column index.
- `double value`
The value.

5.4.1 Detailed Description

A non-zero element of a sparse matrix as a (i, j, value) triplet.

5.4.2 Member Function Documentation

5.4.2.1 operator<()

```
bool diffusion_maps::SparseMatrix::Triplet::operator< (  
    const Triplet & other ) const [inline]
```

Less-than comparison operator. Compares the row and column indices.

Parameters

in	<i>other</i>	The other triple.
----	--------------	-------------------

Returns

True if this triple is less than the other triple in the aforementioned order.

The documentation for this class was generated from the following file:

- include/diffusion_maps/sparse_matrix.hpp

5.5 diffusion_maps::Vector Class Reference

[Vector](#).

```
#include <diffusion_maps/vector.hpp>
```

Public Member Functions

- [Vector](#) ()
Constructs a vector of size 0.
- [Vector](#) (const std::size_t [size](#))
Constructs a vector of size [size](#).
- [Vector](#) (const std::size_t [size](#), const double [value](#))
Constructs a vector of size [size](#) with each element set to [value](#).
- [Vector](#) (const std::initializer_list< double > [list](#))
Constructs a vector from an initializer list.
- [Vector](#) (const [Vector](#) &[other](#))
Copy constructor.
- [Vector](#) ([Vector](#) &&[other](#)) noexcept
Move constructor. The moved-from vector is set to a 0-sized vector.
- virtual [~Vector](#) ()=default
Destructor.
- [Vector](#) & [operator=](#) (const [Vector](#) &[other](#))
Copy assignment operator.
- [Vector](#) & [operator=](#) ([Vector](#) &&[other](#))
Move assignment operator. The moved-from vector is set to a 0-sized vector.
- std::size_t [size](#) () const noexcept
The size of the vector.
- double * [data](#) () noexcept
The data array of the vector.
- const double * [data](#) () const noexcept
The data array of the vector.
- double & [operator\[\]](#) (const std::size_t [index](#))
Gets the element at index [index](#) without bounds checking.
- double [operator\[\]](#) (const std::size_t [index](#)) const
Gets the element at index [index](#) without bounds checking.

- bool `operator==` (const [Vector](#) &other) const
Equality operator.
- bool `operator!=` (const [Vector](#) &other) const
Inequality operator.
- [Vector](#) `operator-` () const
Negation operator.
- [Vector](#) `operator+` (const [Vector](#) &other) const
Addition operator.
- [Vector](#) & `operator+=` (const [Vector](#) &other)
Addition assignment operator.
- [Vector](#) `operator-` (const [Vector](#) &other) const
Subtraction operator.
- [Vector](#) & `operator-=` (const [Vector](#) &other)
Subtraction assignment operator.
- [Vector](#) `operator*` (const double scalar) const
Scalar multiplication operator.
- [Vector](#) & `operator*=` (const double scalar)
Scalar multiplication assignment operator.
- [Vector](#) `operator/` (const double scalar) const
Scalar division operator.
- [Vector](#) & `operator/=` (const double scalar)
Scalar division assignment operator.
- double `dot` (const [Vector](#) &other) const
Dot product.
- double `sq_l2_norm` () const
The squared 2-norm (Euclidean norm) of the vector.
- double `l2_norm` () const
The 2-norm (Euclidean norm) of the vector.
- [Vector](#) `inv_sqrt` () const
Returns a vector where each element is the inverse square root of the corresponding element of this vector.

Protected Attributes

- `std::size_t _size`
The size.
- `std::unique_ptr< double[]> _data`
The data array.

5.5.1 Detailed Description

[Vector](#).

5.5.2 Constructor & Destructor Documentation

5.5.2.1 Vector() [1/5]

```
diffusion_maps::Vector::Vector (
    const std::size_t size ) [inline]
```

Constructs a vector of size `size`.

Parameters

in	<i>size</i>	The size of the vector.
----	-------------	-------------------------

5.5.2.2 Vector() [2/5]

```
diffusion_maps::Vector::Vector (
    const std::size_t size,
    const double value ) [inline]
```

Constructs a vector of size *size* with each element set to *value*.

Parameters

in	<i>size</i>	The size of the vector.
in	<i>value</i>	The value of each element.

5.5.2.3 Vector() [3/5]

```
diffusion_maps::Vector::Vector (
    const std::initializer_list< double > list ) [inline]
```

Constructs a vector from an initializer list.

Parameters

in	<i>list</i>	The initializer list.
----	-------------	-----------------------

5.5.2.4 Vector() [4/5]

```
diffusion_maps::Vector::Vector (
    const Vector & other ) [inline]
```

Copy constructor.

Parameters

in	<i>other</i>	The vector to copy.
----	--------------	---------------------

5.5.2.5 Vector() [5/5]

```
diffusion_maps::Vector::Vector (
    Vector && other ) [inline], [noexcept]
```

Move constructor. The moved-from vector is set to a 0-sized vector.

Parameters

<code>in, out</code>	<code>other</code>	The vector to move.
----------------------	--------------------	---------------------

5.5.3 Member Function Documentation

5.5.3.1 dot()

```
double diffusion_maps::Vector::dot (
    const Vector & other ) const [inline]
```

Dot product.

Parameters

<code>in</code>	<code>other</code>	The vector to dot with.
-----------------	--------------------	-------------------------

Returns

The dot product of the vectors.

Exceptions

<code>std::invalid_argument</code>	If the vectors are not of the same size.
------------------------------------	--

5.5.3.2 inv_sqrt()

```
Vector diffusion_maps::Vector::inv_sqrt ( ) const [inline]
```

Returns a vector where each element is the inverse square root of the corresponding element of this vector.

Returns

The inverse square root of the vector.

5.5.3.3 operator!=(())

```
bool diffusion_maps::Vector::operator!= (
    const Vector & other ) const [inline]
```

Inequality operator.

Parameters

in	<i>other</i>	The vector to compare with.
----	--------------	-----------------------------

Returns

True if the vectors are not equal, false otherwise.

5.5.3.4 operator*()

```
Vector diffusion_maps::Vector::operator* (
    const double scalar ) const [inline]
```

Scalar multiplication operator.

Parameters

in	<i>scalar</i>	The scalar to multiply by.
----	---------------	----------------------------

Returns

The scaled vector.

5.5.3.5 operator*=(())

```
Vector& diffusion_maps::Vector::operator*= (
    const double scalar ) [inline]
```

Scalar multiplication assignment operator.

Parameters

in	<i>scalar</i>	The scalar to multiply by.
----	---------------	----------------------------

Returns

A reference to this vector.

5.5.3.6 operator+()

```
Vector diffusion_maps::Vector::operator+ (
    const Vector & other ) const [inline]
```

Addition operator.

Parameters

in	<i>other</i>	The vector to add.
----	--------------	--------------------

Returns

The sum of the vectors.

Exceptions

<i>std::invalid_argument</i>	If the vectors are not of the same size.
------------------------------	--

5.5.3.7 operator+=()

```
Vector& diffusion_maps::Vector::operator+= (
    const Vector & other ) [inline]
```

Addition assignment operator.

Parameters

in	<i>other</i>	The vector to add.
----	--------------	--------------------

Returns

A reference to this vector.

Exceptions

<i>std::invalid_argument</i>	If the vectors are not of the same size.
------------------------------	--

5.5.3.8 operator-() [1/2]

```
Vector diffusion_maps::Vector::operator- ( ) const [inline]
```

Negation operator.

Returns

The negation of the vector.

5.5.3.9 operator-() [2/2]

```
Vector diffusion_maps::Vector::operator- (
    const Vector & other ) const [inline]
```

Subtraction operator.

Parameters

in	<i>other</i>	The vector to subtract.
----	--------------	-------------------------

Returns

The difference of the vectors.

Exceptions

<i>std::invalid_argument</i>	If the vectors are not of the same size.
------------------------------	--

5.5.3.10 operator-=()

```
Vector& diffusion_maps::Vector::operator-= (
    const Vector & other ) [inline]
```

Subtraction assignment operator.

Parameters

in	<i>other</i>	The vector to subtract.
----	--------------	-------------------------

Returns

A reference to this vector.

Exceptions

<i>std::invalid_argument</i>	If the vectors are not of the same size.
------------------------------	--

5.5.3.11 operator/()

```
Vector diffusion_maps::Vector::operator/ (
    const double scalar ) const [inline]
```

Scalar division operator.

Parameters

in	<i>scalar</i>	The scalar to divide by.
----	---------------	--------------------------

Returns

The scaled vector.

5.5.3.12 operator/=()

```
Vector& diffusion_maps::Vector::operator/= (
    const double scalar ) [inline]
```

Scalar division assignment operator.

Parameters

in	<i>scalar</i>	The scalar to divide by.
----	---------------	--------------------------

Returns

A reference to this vector.

5.5.3.13 operator=() [1/2]

```
Vector& diffusion_maps::Vector::operator= (
    const Vector & other ) [inline]
```

Copy assignment operator.

Parameters

in	<i>other</i>	The vector to copy.
----	--------------	---------------------

Returns

A reference to this vector.

5.5.3.14 operator=() [2/2]

```
Vector& diffusion_maps::Vector::operator= (
    Vector && other ) [inline]
```

Move assignment operator. The moved-from vector is set to a 0-sized vector.

Parameters

<i>in</i> , <i>out</i>	<i>other</i>	The vector to move.
------------------------	--------------	---------------------

Returns

A reference to this vector.

5.5.3.15 operator==()

```
bool diffusion_maps::Vector::operator== (
    const Vector & other ) const [inline]
```

Equality operator.

Parameters

<i>in</i>	<i>other</i>	The vector to compare with.
-----------	--------------	-----------------------------

Returns

True if the vectors are equal, false otherwise.

5.5.3.16 operator[]() [1/2]

```
double& diffusion_maps::Vector::operator[] (
    const std::size_t index ) [inline]
```

Gets the element at index *index* without bounds checking.

Parameters

<code>in</code>	<code>index</code>	The index of the element.
-----------------	--------------------	---------------------------

Returns

The element at index `index`.

5.5.3.17 operator[]() [2/2]

```
double diffusion_maps::Vector::operator[] (
    const std::size_t index ) const [inline]
```

Gets the element at index `index` without bounds checking.

Parameters

<code>in</code>	<code>index</code>	The index of the element.
-----------------	--------------------	---------------------------

Returns

The element at index `index`.

The documentation for this class was generated from the following file:

- [include/diffusion_maps/vector.hpp](#)

Chapter 6

File Documentation

6.1 include/diffusion_maps/diffusion_maps.hpp File Reference

Diffusion maps algorithm.

```
#include <functional>
#include <memory>
#include <random>
#include "diffusion_maps/matrix.hpp"
#include "diffusion_maps/vector.hpp"
```

Namespaces

- [diffusion_maps](#)

Namespace for everything related to diffusion maps.

Functions

- `template<typename R >`
Matrix [diffusion_maps::diffusion_maps](#) (const Matrix &data, std::size_t n_components, const std::function<double(const Vector &, const Vector &)> &kernel, double diffusion_time, R &rng, double kernel_epsilon=DEFAULT_KERNEL_EPSILON, double eig_solver_tol=DEFAULT_EIG_SOLVER_TOL, unsigned eig_solver_max_iter=DEFAULT_EIG_SOLVER_MAX_ITER)

Diffusion maps.

Variables

- `constexpr double diffusion_maps::DEFAULT_KERNEL_EPSILON = 1e-6`
Default kernel epsilon for the [diffusion_maps\(\)](#) function.
- `constexpr double diffusion_maps::DEFAULT_EIG_SOLVER_TOL = 1e-6`
Default tolerance of the eigendecomposition solver for the [diffusion_maps\(\)](#) function.
- `constexpr unsigned diffusion_maps::DEFAULT_EIG_SOLVER_MAX_ITER = 100000`
Default maximum number of iterations of the eigendecomposition solver for the [diffusion_maps\(\)](#) function.

6.1.1 Detailed Description

Diffusion maps algorithm.

6.2 include/diffusion_maps/kernel.hpp File Reference

Diffusion kernels.

```
#include "diffusion_maps/vector.hpp"
```

Classes

- class [diffusion_maps::kernel::Gaussian](#)
Gaussian kernel.

Namespaces

- [diffusion_maps](#)
Namespace for everything related to diffusion maps.
- [diffusion_maps::kernel](#)
Diffusion kernels.

6.2.1 Detailed Description

Diffusion kernels.

6.3 include/diffusion_maps/matrix.hpp File Reference

Matrix.

```
#include <cstddef>  
#include <memory>  
#include <variant>  
#include "diffusion_maps/internal/utils.hpp"  
#include "diffusion_maps/vector.hpp"
```

Classes

- class [diffusion_maps::Matrix](#)
Matrix of doubles that may or may not own its data.

Namespaces

- [diffusion_maps](#)

Namespace for everything related to diffusion maps.

6.3.1 Detailed Description

Matrix.

6.4 include/diffusion_maps/sparse_matrix.hpp File Reference

Sparse matrix.

```
#include <algorithm>
#include <cstddef>
#include <memory>
#include <stdexcept>
#include <tuple>
#include <vector>
#include "diffusion_maps/vector.hpp"
```

Classes

- class [diffusion_maps::SparseMatrix](#)
Sparse matrix in the CSR format.
- class [diffusion_maps::SparseMatrix::Triplet](#)
A non-zero element of a sparse matrix as a (i, j, value) triplet.

Namespaces

- [diffusion_maps](#)

Namespace for everything related to diffusion maps.

6.4.1 Detailed Description

Sparse matrix.

6.5 include/diffusion_maps/vector.hpp File Reference

Vector.

```
#include <algorithm>
#include <cmath>
#include <cstddef>
#include <initializer_list>
#include <memory>
#include <stdexcept>
```

Classes

- class [diffusion_maps::Vector](#)
Vector.

Namespaces

- [diffusion_maps](#)
Namespace for everything related to diffusion maps.

6.5.1 Detailed Description

Vector.

Index

- diffusion_maps, 7
 - diffusion_maps, 8
- diffusion_maps::kernel, 9
- diffusion_maps::kernel::Gaussian, 11
 - Gaussian, 11
 - with_gamma, 12
 - with_sigma, 12
- diffusion_maps::Matrix, 12
 - Matrix, 13, 14
 - operator(), 14
 - row, 15
- diffusion_maps::SparseMatrix, 15
 - operator*, 18
 - operator=, 18
 - SparseMatrix, 17
- diffusion_maps::SparseMatrix::Triplet, 19
 - operator<, 19
- diffusion_maps::Vector, 20
 - dot, 23
 - inv_sqrt, 23
 - operator!=, 23
 - operator*, 24
 - operator*=: 24
 - operator+, 25
 - operator+=, 25
 - operator-, 25, 26
 - operator-=, 26
 - operator/, 27
 - operator/=, 27
 - operator=, 27, 28
 - operator==, 28
 - operator[], 28, 29
 - Vector, 21, 22
- dot
 - diffusion_maps::Vector, 23
- Gaussian
 - diffusion_maps::kernel::Gaussian, 11
- include/diffusion_maps/diffusion_maps.hpp, 31
- include/diffusion_maps/kernel.hpp, 32
- include/diffusion_maps/matrix.hpp, 32
- include/diffusion_maps/sparse_matrix.hpp, 33
- include/diffusion_maps/vector.hpp, 33
- inv_sqrt
 - diffusion_maps::Vector, 23
- Matrix
 - diffusion_maps::Matrix, 13, 14
- operator!=
 - diffusion_maps::Vector, 23
- operator<
 - diffusion_maps::SparseMatrix::Triplet, 19
- operator*
 - diffusion_maps::SparseMatrix, 18
 - diffusion_maps::Vector, 24
- operator*=
 - diffusion_maps::Vector, 24
- operator()
 - diffusion_maps::Matrix, 14
- operator+
 - diffusion_maps::Vector, 25
- operator+=
 - diffusion_maps::Vector, 25
- operator-
 - diffusion_maps::Vector, 25, 26
- operator=-
 - diffusion_maps::Vector, 26
- operator/
 - diffusion_maps::Vector, 27
- operator/=
 - diffusion_maps::Vector, 27
- operator=
 - diffusion_maps::SparseMatrix, 18
 - diffusion_maps::Vector, 27, 28
- operator==
 - diffusion_maps::Vector, 28
- operator[]
 - diffusion_maps::Vector, 28, 29
- row
 - diffusion_maps::Matrix, 15
- SparseMatrix
 - diffusion_maps::SparseMatrix, 17
- Vector
 - diffusion_maps::Vector, 21, 22
- with_gamma
 - diffusion_maps::kernel::Gaussian, 12
- with_sigma
 - diffusion_maps::kernel::Gaussian, 12